Evaluation of liquefaction probability of earth-fill dam over next 50 years using geostatistical method based on CPTU

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**ABSTRACT:** In this paper, the spatial distribution of the liquefaction probability inside the studied dam was calculated from CPTUs including conversion errors and the spatial variability of the soil parameters. In addition, based on the seismic hazard at the studied site and the fragility, the spatial average of the liquefaction probability over the next 50 years was evaluated. Although the CPTU is often preferable for identifying the liquefaction probability, the CPTU is still not widely used in Japan. Therefore, the focus will be placed here on the SPT N-value and the fines content, $F_r$, because the majority of the accumulated site characterization data in Japan consists of SPT N-values and $F_r$. Utilizing the conditional simulation, the spatial distribution of the expected values for $F_r$ and $N_{SPT}$ inside the dam were calculated with high spatial resolution. Based on the results of the simulation the scale of the weak areas and the spatial continuity of the soil profile of the dam were clarified.

**Keywords:** liquefaction; cone penetration test; seismic hazard; geostatistics; spatial variability

1. **INTRODUCTION**

There are many earth-fill dams for agriculture in Japan. Most of them were constructed 150–500 years ago and have become old and decrepit. In addition, over the next 30 years, the probability of an earthquake occurring in the Nankai Trough is reported to be about 70%. And it is predicted that the magnitude of this earthquake will be as large as 9.0. Such an earthquake would affect a wide area from western to central Japan. In the 2011 off the Pacific coast of Tohoku Earthquake, the failure of the Fujinuma Dam was found to have been caused by liquefaction inside the dam (e.g., Tatsuoka et al., 2017; Ono et al., 2011). Since then, the design guidelines for earth-fill dams for irrigation have demanded an evaluation of the probable liquefaction damage (Ministry of Agriculture, Forestry, and Fisheries of Japan, 2015). For the above-mentioned reasons and to prevent the failure of dams against great earthquakes, the efficient improvement of the dams is required within a limited time and with a limited budget. Evaluating and comparing the seismic risk of various dams enables a quantitative prioritization of the dams such that a decision can be made on which dams among many are to be improved. In general, the seismic risk is expressed by the multiplication of the failure probability by the cost of failure. Therefore, a new procedure is proposed here for evaluating the liquefaction probability of a dam against a potential Nankai Trough earthquake.

The novelty of the proposed work comes from the statistical modeling of the SPT (Standard penetration test) $N$-value and $F_r$ based on the CPTUs (Cone penetration tests), including the conversion of the measured values from the CPTUs into the SPT $N$-value and $F_r$, for evaluating the liquefaction probability. A unique feature of the proposed work is its potential capability to take into account the accumulated site characterization data, such as the SPT $N$-value and $F_r$, adjacent to the studied site. An illustrative example assessing the liquefaction probability of an earth-fill dam in Japan is presented to demonstrate the capability of the proposed method.

2. **SITE INVESTIGATION**

An earth-fill dam in Hiroshima Prefecture, Japan is analyzed. The earth-fill dam is one of the dams for which there is a fear of liquefaction damage should a Nankai Trough earthquake occur. In Japan, to design countermeasures against the liquefaction of an earth-fill dam, the $N$-value obtained from the SPT is generally used. In the Japanese design code for earth-fill dams for irrigation, the liquefaction resistance factor $F_L$ method, originally based on the study of Iwasaki et al. (1984), is used. In Iwasaki’s method, the $N$-value and fines content $F_r$ are utilized to calculate $F_L$. Therefore, the measured values from CPTUs on the dam are firstly converted into the soil behavior type index, $I_s$, proposed by Robertson and Wride (1998). Then, $I_s$ is used to obtain the $N$-value and $F_r$ by utilizing the conversion formulas which were originally proposed by Suzuki et al. (2003).

The CPTU is employed to obtain several soil parameters, such as corrected cone resistance $q_c$, measured sleeve friction $f_s$, and pore water pressure $u$ in short intervals. CPTUs were conducted at 15 points at the top of the dam at intervals of 2 m along the crest, as shown in Figure 1. The geological cross section at the studied site is given in Figure 2.

The CPTU results can be used to estimate the ground composition. To conduct the soil classification based on the CPTUs, the soil behavior type index, $I_s$, was proposed, as seen in Eq. (1) (Robertson and Wride, 1998).
As a result, equivalent to included. However, in Eqs. (2003), was derived from the data included in Suzuki et al. (2003), while Eq. (4) was proposed by Suzuki et al. (2003), which includes two normalized parameters, \( Q \) and \( F \), given by Eqs. (2) and (3) (Robertson, 1990), respectively:

\[
I_c = \left[ \frac{3.47 - \log Q}{1.22 + \log F} \right]^2 \\
Q = \frac{q_t - \sigma_{o0}}{\sigma_{o0}} \\
F = \frac{f_s}{\sqrt{q_t - \sigma_{o0}}} \times 100\%
\]

where \( Q \) is the normalized CPT penetration resistance, \( F \) is the normalized friction ratio (%), \( q_t \) is the corrected cone resistance (kPa), \( f_s \) is the measured sleeve friction (kPa), and \( \sigma_{o0} \) and \( \sigma_{o0} \) are the total and the effective overburden stresses (kPa), respectively. Corrected cone resistance \( q_t \) and measured sleeve friction \( f_s \) are directly measured values in the CPTUs.

Based on \( I_c \) and \( q_t \) obtained from the CPTUs, the CPTU \( N \)-value, \( N_c \), and the fines content, \( F_{ck} \), obtained from \( I_c \), can be estimated by the following equations. Eq. (4) was proposed by Suzuki et al. (2003), while Eq. (5) was derived from the data included in Suzuki et al. (2003):

\[
N_c = 0.341 \frac{I_c^{1.94}}{\left( q_t - 0.2 \right)^{0.2841(1)}} \quad \left( q_t > 0.2 \text{MPa} \right) \\
N_c = 0 \quad \left( q_t \leq 0.2 \text{MPa} \right)
\]

\[
F_{ck} = 1.01 \times 10^{-0.0024} \quad \left( \%ight)
\]

Since the above-mentioned conversion formulas are based on experimental data, conversion errors could be included. However, in Eqs. (4) and (5), the conversion errors are not explicitly considered. Thus, the conversion errors are quantified based on measured data.

Based on the idea of Suzuki et al. (2003), that \( N_c \) is equivalent to \( N_{SPT} \), Fig. 3 shows the relationship between \( N_c \) and \( N_{SPT} \) included in the data of earth-fill dams. As a result, \( N_c \) is converted into \( N_{SPT} \) by the following equation considering the conversion error:

\[
N_{SPT} = N_c (1 + 0.62 \varepsilon)
\]

where error term \( \varepsilon \) is assumed to obey standard normal distribution \( N(0,1) \). In Eq. (6), \( N_c \) is assumed to be equal to \( N_{SPT} \), and the quantity of the conversion error is given by the coefficient of variation calculated from the values of the ratio of \( N_{SPT} \) to \( N_c \). In addition, the conversion error is proportional to \( N_c \) and corresponds to 0 when \( N_c = 0 \).

The relationship between fines content \( F_{ck} \), obtained from \( I_c \), and the proper fines content, \( F_{ck} \) is given in Fig. 4. \( F_{ck} \) is converted into \( F_c \) by the following equation considering the conversion error:

\[
F_c = 2 - 2 \left( 2 - F_{ck} \right) \left( 1 + 0.598 \varepsilon \right)
\]

where error term \( \varepsilon \) is assumed to obey standard normal distribution \( N(0,1) \). \( F_{ck} \) is assumed to be equal to \( F_c \), and the quantity of the conversion error is given by the coefficient of variation calculated from the values of the ratio of \( F_{ck} \) to \( F_c \). In addition, the conversion error is in inverse proportion to \( F_c \) and corresponds to 0 when \( F_c = 2 \).

### 3. STATISTICAL MODEL

**IDENTIFICATION OF STUDIED DAM**

A Statistical models of soil parameters are useful for visualizing the spatial variability of the soil parameters. This is because the soil parameters for the points where test results do not exist can be estimated using the statistical models. The statistical models of the CPTU results are determined based on a geostatistical method (Journel and Huijbregts, 1978) and random field theory.
parameters, be of an exponential type and composed of several (Akaike, 1974) Akaike’s information criterion (MAIC) procedure log the standard deviations, and the covariance functions of information criterion (AIC) is used. The mean functions, mo determined for CPT maximum likelihood (MLE), the statistical models are Kulhawy, 199 parameters (e.g., a normal random variable. It is assumed that variable cIc defined by Eq. 8 is commonly used to model the soil trend function by CPT explicitly. Since the densely obtained data on the dam variability can be introduced into the statistical models liquefaction probability have spatial variability, the Although the soil parameters utilized to calculate the liquefaction probability have spatial variability, the variability can be introduced into the statistical models explicitly. Since the densely obtained data on the dam by CPTUs are converted into N-values and fines content Fc, a large amount of N-values and Fc data can be utilized for statistical model identification.

The representative variable for soil parameter s is defined by Eq. (8) as the function of location X = (x, z).

It is assumed that variable s is expressed as the sum of trend function m and fluctuation component U, which is a normal random variable.

s(X) = m(X) + U(X) (8)

The method is commonly used to model the soil parameters (e.g., Vanmarcke, 1983; Phoon and Kulhawy, 1999). Herein, based on the method of maximum likelihood (MLE), the statistical models are determined for CPTU N-value logNc and fines content logFc. The detailed procedure for the statistical model identification is described in Nishimura (2016). In the model identification based on MLE, the Akaike’s information criterion (AIC) is used. The mean functions, the standard deviations, and the covariance functions of logNc and logFc are determined by the minimum Akaike’s information criterion (MAIC) procedure (Akaike, 1974). The covariance function is assumed to be of an exponential type and composed of several parameters, such as the standard deviation, the correlation distance of horizontal and depth directions, and the nugget effect parameter. Table 1 presents the mean function and the covariance function of logNc and logFc estimated by MAIC. As shown in Table 1, lateral correlation distance l in the model of logNc, obtained by MAIC, is not reasonable, because the value is identified as being the lower boundary value of 0.01 m. In the MAIC, the correlation structure of the multi-points distributed multi-dimensionally are evaluated simultaneously, and this procedure sometimes creates difficulty. On the other hand, since calculating the semi-variogram (Journel and Huijbregts, 1976) is the method for identifying the correlation distance one-dimensionally, it is easier to use the semi-variogram than the MAIC for finding the correlation distance. The semi-variograms of horizontal direction l have depth direction l are defined by the following equations, respectively:

\[
\gamma_s(x, z) = \frac{1}{2D_x} \sum_{j=1}^{D_x} \left[ U(x, z) - U(x + x_j, z) \right]^2
\]

\[
\gamma_s(z) = \frac{1}{2D_z} \sum_{j=1}^{D_z} \left[ U(z, z) - U(z + z_j, z) \right]^2
\]

where \(D_x\) and \(D_z\) denote the number of combinations of \(U(x, z) - U(x + x_j, z)\) and \(U(z, z) - U(z + z_j, z)\), respectively, in which \(x_j\) and \(z_j\) mean the separation distances in the horizontal and vertical

<table>
<thead>
<tr>
<th>Table 1 Statistical models of logNc and logFc estimated by MAIC.</th>
<th>Covariance function ((i, j = 1, 2, \ldots, M))</th>
</tr>
</thead>
<tbody>
<tr>
<td>logNc</td>
<td>(m = 0.370 - 0.012x - 0.030z + 0.001x^2 + 0.005z^2 - 0.001xz)</td>
</tr>
<tr>
<td></td>
<td>(C = \begin{bmatrix} C_{ij} \end{bmatrix} = 0.246 \exp \left[ - \frac{</td>
</tr>
<tr>
<td>logFc</td>
<td>(m = 0.874 + 0.021x + 0.217z - 0.001x^2 - 0.019z^2 - 0.0001xz)</td>
</tr>
<tr>
<td></td>
<td>(C = \begin{bmatrix} C_{ij} \end{bmatrix} = 0.123 \cdot 0.688 \exp \left[ - \frac{</td>
</tr>
</tbody>
</table>

\(m\) : Mean function, \(x\) : Horizontal coordinate (m), \(z\) : Depth (m)
directions. $U(x_i)$ is $|x_i - x_j|$ away from $U(x_i + x_i - x_j)$ at the same depth, and similarly, $U(z_i)$ is $|z_i - z_j|$ away from $U(z_i + z_i - z_j)$ at the same horizontal coordinate. Figs. 5 and 6 show the semi-variograms of logNc and logFdc for the horizontal and depth directions, respectively, of the dam. In the calculation of semi-variograms, the measured values are assumed to be standard normal distribution $N(0, 1)$. For example, logNc is standardized as $f = \frac{(\log N_c - m)}{\sigma}$ to remove the trend where $m$ is the mean value and $\sigma$ is the standard deviation; they are obtained from MAIC. In addition, in order to set the $f$ values to be $N(0, 1)$ with certainty, the following equation is used here:

$$Y = \Phi^{-1} \left[ F(f) \right]$$  \hspace{1cm} (10)

where $Y$ is the cumulative distribution function of $f$ and $\Phi$ is the standard normal distribution function. To identify the geostatistical parameters of a standardized value $Y$, the approximation curve is simply modeled by an exponential function as the following equations:

$$\gamma(x) = C_0 + C_1 \left[ 1 - \exp \left( -|x|/l_x \right) \right] \quad (i \neq j)$$

$$\gamma(z) = C_0 + C_1 \left[ 1 - \exp \left( -|z|/l_z \right) \right] \quad (i \neq j)$$

$$\gamma(0) = \gamma(0) = 0$$

where, $C_0$ and $C_0$ are the parameters used for the nugget effect in the $x$ and $z$ directions, respectively, while $C_1$ and $C_1$ are the parameters used to express the shape of the semi-variogram functions. Based on the semi-variograms of the $x$ and $z$ directions, the covariance matrix $C$ composed of the standardized values is assumed to have the following form:

$$C = \begin{bmatrix} C_{xx} & C_{xz} \\ C_{xz} & C_{zz} \end{bmatrix}$$

$$C_{xx} = \begin{bmatrix} \{x_i - x_j \}^2 & 0 \\ 0 & \{z_i - z_j \}^2 \end{bmatrix}$$

$$C_{xz} = \begin{bmatrix} 0 & \{x_i - x_j \} \{z_i - z_j \} \end{bmatrix}$$

$$C_{zz} = \begin{bmatrix} 0 & \{z_i - z_j \} \{x_i - x_j \} \end{bmatrix}$$

$$C = \sigma_x^2 \begin{bmatrix} C_{xx} & C_{xz} \\ C_{xz} & C_{zz} \end{bmatrix} \quad (i \neq j)$$

As shown in Figs. 5 and 6, the approximation curves roughly correspond to the observed values. These approximation curves are derived by the least squares method, and finally, parameters $C_{0x}$, $C_{1x}$, $C_{0z}$, $C_{1z}$, $l_x$, and $l_z$ are determined. The separation distances of the data, $\Delta x = |x_i - x_j|$ and $\Delta z = |z_i - z_j|$, are less than 6 m in the horizontal direction and less than 0.9 m in the depth direction, and are applied to identify the approximate functions, since the accuracy of the semi-variograms is high within the range of small values for $l_x$ and $l_z$. Within the ranges of 10 m for the horizontal direction and 1 m for the vertical direction, the exponential correlation function simulates the actual correlations very well. For long separation distances, however, the variogram value should converge to 1.0 and the exponential function is appropriate. Table 2 shows the constants determined by the semi-variograms. The lateral correlation distance obtained from the semi-variograms is about 10 times that of the vertical one. The identified correlation distances are supposed to be reasonable, because this relationship agrees with the published values (Nishimura, 2007; Phoon and Kulhawy, 1999).

### 4. Interpolation of Measured Value of CPTUs

Since the data measured by the CPTUs are point estimation values, the interpolation of these values is required for visualizing the spatial variability of the soil parameters. Thus, the geostatistical software library GSLIB (Deutsch and Journel, 1992) is used as a conditional simulation tool. In the conditional simulation, the realizations of the simulation are based on the statistical models of the soil parameters which are characterized by their first two moments and their covariance function. The realizations generated by the simulation are conditioned by the measured data, and the values of the realizations coincide with the measured values at the measuring points.

Utilizing the simulation tool, the cross section of the studied dam along the embankment axis is analyzed. The cross section is meshed into several grids at intervals of 1 m in the horizontal direction and 0.05 m in the depth direction. The grid spacing is selected such that it corresponds to the intervals of the CPTU data. The Monte Carlo method is repeated 2000 times to evaluate the spatial distribution of the expected values for $N_{SPT}$ and $F_c$ at the grid points. In addition, the validity of the interpolated values calculated from the conditional simulation was examined, and the results have been published in Imaide et al. (2018) and Imaide et al. (2019).

The statistical models for logNc and logFdc introduced into the simulation, are summarized in Table 3. In this table, the mean functions and the standard deviations are derived from MAIC, and the covariance functions are determined by the semi-variograms. The covariance function is assumed to be an exponential type of function.

Figs. 7 and 8 present the spatial distributions of the statistical values inside the dam derived from the conditional simulation. Figs. 7(a) and 8(a) correspond to the spatial distributions of the expected values for $F_c$ and $N_{SPT}$. Figs. 7(b) and 8(b) correspond to the spatial distributions of the standard deviations for $F_c$ and $N_{SPT}$, and Figs. 7(c) and 8(c) correspond to the spatial

| Table 2 Constants of covariance functions of logNc and logFdc determined by semi-variograms. |
|-----------------|-----------------|-----------------|-----------------|
| logNc           | C0x=0.48, C0z=0.08 | C1x=0.52, C1z=0.92 | l=2.42, l=0.29 |
| logFdc          | C0x=0.57, C0z=0.40 | C1x=0.43, C1z=0.60 | l=9.17, l=0.82 |

C.L. : Correlation length
Table 3. Statistical models for log\(N_c\) and log\(F_{ci}\) introduced into the simulation.

<table>
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<th>Mean function</th>
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<td>(\log N_c)</td>
<td>(m = 0.370 - 0.012x - 0.030z + 0.001x^2 + 0.005z^2 - 0.001xz)</td>
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<td>(\log F_{ci})</td>
<td>(m = 0.874 + 0.021x + 0.217z - 0.001x^2 - 0.019z^2 - 0.0001xz)</td>
<td>(\sigma = 0.123)</td>
</tr>
</tbody>
</table>

Covariance function \((i, j = 1, 2, \ldots, M)\):

\[
\begin{align*}
\log N_c & : C_{ij} = \sigma^2 \cdot N_c \cdot \exp\left(-\frac{|x_i - x_j|^2 + |z_i - z_j|^2}{2.42 - |z_i - z_j|^2}/0.29\right) \quad (i \neq j) \\
N_c & : 0.475 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
N_c & : 0.519 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
N_c & : 0.917 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
C & : 0.246 \quad (i = j)
\end{align*}
\]

\[
\begin{align*}
\log F_{ci} & : C_{ij} = \sigma^2 \cdot N_c \cdot \exp\left(-\frac{|x_i - x_j|^2 + |z_i - z_j|^2}{9.17 - |z_i - z_j|^2}/0.82\right) \quad (i \neq j) \\
N_c & : 0.256 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
N_c & : 0.429 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
N_c & : 0.598 \left(|x_i - x_j| = 0, |z_i - z_j| = 0\right) \\
C & : 0.123 \quad (i = j)
\end{align*}
\]

\(m\) : Mean function, \(\sigma\) : Standard deviation, \(x\) : Horizontal coordinate (m), \(z\) : Depth (m), \(M\) : Number of test points, \(N_c\) : Nugget effect.

According to Figure (a), the soil which comprises about 35-40\% \(F_c\) is distributed in the dominant area of the dam. The soil profile for this area is categorized as distributions of the probability of \(F_c < 35\%\) and \(N_{SPT} < 2\), respectively.
intermediate soil; it consists of sandy and fine materials. The area of $x = 10-17$ m and $z = 3-9$ m has a relatively high $F_L$ (about 50%), because this area is located above the sluiceway inside the dam. Figure (b) shows the spatial distribution of the standard deviation of $F_L$, including the conversion error given in Eq. (7). Since the conversion error is considered, the standard deviation is large in the dominant area inside the dam, and the value is up to about 30%. In Figure (c), the probability of $F_L < 35\%$ is more than 0.5 in the dominant area inside the dam, because the standard deviation is large.

According to Figure (a), the overall $N$-value inside the dam is relatively small. In particular, there are weak areas around $x = 0-28$ m and $z = 3$ m and $x = 10-17$ m and $z = 3-9$ m. Figure (b) shows the spatial distribution of the standard deviation of $N_{SPT}$, including the conversion error, as shown in Eq. (6). The standard deviations are relatively small at the test points where the expected values are small. Based on Figure (c), the particularly weak areas inside the dam are identified. These areas are located around $x = 10-15$ m and $z = 3-6$ m and $x = 0-15$ m and $z = 7-8$ m.

5. CALCULATION OF LIQUEFACTION PROBABILITY

The effects of liquefaction damage on structures must be quantitatively clarified in order to establish the proper seismic design for structures. Liquefaction resistance factor $F_L$ is used to evaluate liquefaction probability $P_f$. Liquefaction resistance factor $F_L$ (Iwasaki et al., 1984) is calculated by the following equations:

$$F_L = \frac{R(N_{SPT}, F_c)}{L(a_{max})}$$

(13)

$$F_L = F_L(x, z, a_{max}, N_{SPT}, F_c) = R(x, z, N_{SPT}, F_c) / L(z, a_{max})$$

(14)

where $R$ is the liquefaction resistance and $L$ is the dynamic load. The empirical equations to calculate $F_L$ are shown in Japan Road Association (2012) in detail. The relationship between factor $F_L$ and $P_f$ is given based on many in-situ investigations (Iwasaki et al., 1984), as shown in Fig. 9. The Iwasaki’s relationship is utilized to transform $F_L$ into $P_f$ by function $g$, as shown in Eq. (15).

$$P_f(x, z, a_{max}) = g(F_L) = g(x, z, a_{max}, N_{SPT}, F_c)$$

(15)

for which function $g$ is given in Fig 9. In the numerical analysis, function $g$ is introduced as a digital value.

In the analysis, random variables generated from the conditional simulation tool SGSIM, which uses the Ordinary Kriging theory and is included in GSLIB (Deutsch and Journel, 1992), are assigned to $N_{SPT}$ and $F_c$. In this research, the conditional simulation "SGSIM" is used, since the evaluation of the liquefaction probability includes a complicated process. Since the Monte Carlo method is repeated 2000 times in the analysis, the expected value for liquefaction probability $P_{fE}$ as the fragility is obtained at the grid points of the analyzed cross section by the following equation. Herein, the fragility means the liquefaction probability over the next 50 years as corresponds to $a_{max}$.

$$P_{fE}(x, z, a_{max}) = E\{g(F_L(x, z, a_{max}, N_{SPT}, F_c))\}$$

(16)

Considering all the probabilistic variables, namely, $N_{SPT}$, $F_c$, and the peak ground acceleration of the dam over the next 50 years, $a_{max}$, the liquefaction probability over the next 50 years is calculated by Eq. (17) at the output points of the simulation $(x, z)$ inside the dam.

$$P_{fE50}(x, z) = \frac{\int_0^{a_{max}} dH(a_{max}) P_{fE}(x, z, a_{max}) da_{max}}{a_{max}}$$

(17)

where $P_{fE50}$ is the liquefaction probability over the next 50 years at $(x, z)$ inside the dam and $H$ is the seismic hazard curve of Nankai Trough earthquake of studied dam.

To compare the degree of vulnerability against liquefaction among many dams all over Japan, the spatial average of $P_{fE}$ and $P_{fE50}$ of a dam could be useful. This is because the local liquefaction is difficult to compare quantitatively. The spatial average of $P_{fE}$ is obtained for evaluating the fragility of the whole dam by Eq. (18).

$$\overline{P_{fE}}(a_{max}) = \frac{1}{L_x} \int_{L_y} P_{fE}(x, z, a_{max})(10-0.5z)dz \dx$$

(18)

$\overline{P_{fE}}$ is the spatial average of the expected value for the liquefaction probability of the whole dam, and $L_x$ is the horizontal length of the site investigation at the studied site, namely, 28 m. It is reasonable that the effect of liquefaction near the surface is more important than that in deeper areas. Therefore, $P_{fE}$ is weighed based on the linear function of the depth direction. The
weight decreases in the direction of depth and corresponds to 0 at $z=20$ m. This assumption is determined based on the results of the site investigations shown in Iwasaki et al. (1984).

The spatial average of $P_{\overline{E_{50}}} \max$ is calculated with the following equation:

$$\overline{P}_{\overline{E_{50}}} = \int_{0}^{\infty} \frac{dH}{da_{\max}} \overline{P}_{\overline{E_{50}}} (a_{\max}) da_{\max}$$

(19)

where $\overline{P}_{\overline{E_{50}}} \max$ is the liquefaction probability of the whole dam over the next 50 years.

6. EVALUATION OF LIQUEFACTION PROBABILITY OVER NEXT 50 YEARS

In Figure 11, the seismic hazard curve at the crest of the dam, shown in Fig. 10, and the fragility curve of the whole dam, calculated by Eq. (18), are summarized. The seismic hazard shown in Fig. 11 is relatively sensitive to the span of $a_{\max}$ from 111 to 223 gal. In addition, the fragility is relatively sensitive to the span of $a_{\max}$ from 70 to 203 gal. For $a_{\max}$ greater than 265 gal, the fragility becomes greater than 95%.

Fig. 12 shows the cumulative distribution function of the liquefaction probability of the whole dam over the next 50 years, $\overline{P}_{\overline{E_{50}}} \max$, derived from Eq. (19). In the calculation of $\overline{P}_{\overline{E_{50}}} \max$, the convolution integral of the seismic hazard, $H$, and the fragility curve, shown in Fig. 11, are employed. As a result, $\overline{P}_{\overline{E_{50}}} \max$, which is the spatial average of the $P_{\overline{E_{50}}} \max$ of the dam, is evaluated as 61%. The value of the vertical axis in Fig. 12 shows the exceedance probability over the next 50 years; it increases about 32% between the peak ground acceleration, $a_{\max}$, of 160 and 224 gal. It is derived from the condition whereby not only is the fragility high, but the probability of the occurrence of an earthquake is high in that range of $a_{\max}$ as shown in Fig. 11. As $\overline{P}_{\overline{E_{50}}} \max=61\%$ is not small, the liquefaction probability of the dam against a Nankai Trough earthquake cannot be ignored.

Fig. 13 shows the spatial distribution of the expected value of the liquefaction probability when $a_{\max}$ is equivalent to 140 gal. The value of $a_{\max}=140$ gal is predicted to be nearly 50% at the site over the next 50 years. $N_{SPT}$ is relatively small at $x=0-16$ m, $z=7-8$ m and at $x=10-13$ m, $z=3-6$ m, as shown in Fig. 8(a). Corresponding to the tendency of $N_{SPT}$, the liquefaction probability in these areas is relatively high.

Fig. 14 shows the spatial distribution of $P_{\overline{E_{50}}} \max$ inside the dam calculated by Eq. (17). According to Fig. 14, the liquefaction probability over the next 50 years is relatively high at locations similar to those seen in Fig. 13. Based on the results shown in Figs. 13 and 14, it seems that the $N_{SPT}$ values have a greater influence on the liquefaction probability.

The number of CPTUs used in this case is quite large; and therefore, the example presented here is exceptional. For real applications, the investigation costs should be considered in many cases. As for cost-effective approaches, the mixed approach of the soundings and geophysical surveys (e.g., Nishimura, et al., 2016) can be considered. As other practical concepts, the extension and utilization of the database for the statistical values of soil parameters (e.g., Ching and Phoon, 2019) can be mentioned. In Ching’s approach, the information from the database is mixed and used with the values measured in-situ to characterize the soil properties of the site in question.

Since the CPTUs were conducted in short intervals for examining the spatial variability of $N_{SPT}$
and \( F_e \), it was possible to evaluate in detail the location and the scale of the weak areas against the liquefaction inside the dam over the next 50 years. Based on the spatial distribution of the liquefaction probability, the diagnosis of an earth-fill dam against liquefaction is made properly. In addition, introducing the seismic hazard and the fragility curve into the calculation of the liquefaction probability of an earth-fill dam, the liquefaction hazard during the selected time period could be incorporated. Using the seismic hazard and the fragility curve of the dams, if the dams are located in different parts of Japan, the priority of the improvements to be made to them against the probable liquefaction damage of each dam can be compared based on the proposed method. Therefore, the proposed method for evaluating the liquefaction probability of an earth-fill dam can provide useful information for determining the order of priority among the many dams in Japan in terms of making improvements to them.

7. Conclusions

The spatial distribution of the liquefaction probability inside the studied dam has been calculated in detail from CPTUs including conversion errors and the spatial variability of the soil parameters. In addition, based on the seismic hazard at the studied site and the fragility of the dam, the spatial average of the liquefaction probability of the dam over the next 50 years has been evaluated. The concluding remarks are summarized below.

1. The conversion errors, from the CPTU \( N_v \), to the SPT \( N_v \), from the fines content, \( F_{dc} \), obtained from \( I_s \) to the proper fines content, \( F_e \), have been quantified, respectively, in the conversion formulas proposed in this study. According to the results of a conditional simulation with the conversion errors, the standard deviation of \( F_e \) has been calculated as nearly 30% in the dominant area of the studied dam.

2. The spatial structures of \( \log N_v \) and \( \log F_e \) have been determined based on the densely measured data from the CPTUs. Since the CPTUs were conducted with 2-m intervals in the horizontal direction, an extensive data set of \( F_e \) has been estimated from the CPTUs through the use of conversion formulas. As a result, the correlation distances of \( \log N_v \) and \( \log F_e \) have been reasonably identified, because the horizontal value was about 10 times that of the vertical one.

3. Utilizing the conditional simulation, the spatial distribution of the expected values for \( F_e \) and \( N_{SPT} \), the standard deviation of \( F_e \) and \( N_{SPT} \), and the probability that the simulated values inside the dam would be lower than the prescribed threshold values for \( F_e \) and \( N_{SPT} \), respectively, have been visualized in detail. These results clarify the scale of the weak area and the spatial continuity of the soil profile inside the dam.

4. The seismic hazard at the studied site and the fragility against the liquefaction of the dam have been introduced into the evaluation of the liquefaction probability of the dam over the next 50 years. As a result, it has been confirmed that the spatial average of the liquefaction probability of the dam over the next 50 years has been calculated as 61%. Although the desired value of the liquefaction probability of a dam depends on the situation, the liquefaction probability of dams calculated by the proposed method can offer supporting evidence for decision-making in terms of improving the dams.

Nevertheless, dense data are required to identify the spatial structure of the soil parameters in order to evaluate the liquefaction probability of a dam, and the number of test data is not enough for the statistical modeling. Therefore, to calculate the liquefaction probability with limited information, a database for the spatial structure of the soil parameters needs to be developed. Although the data obtained from the SPT or laboratory tests are generally sparse for characterizing the statistical model, an extensive data set on the soil parameters can be obtained by applying conversion formulas to the measured data from CPTUs. Thus, the proposed method could be useful for evaluating the spatial structure of the soil parameters properly and for developing a database for the spatial structure of the soil parameters.

A common problem for evaluating the liquefaction probability of an earth-fill dam is the limited time and the limited budget for site investigations. It has been shown that the proposed method can accurately evaluate the liquefaction probability of a dam based on the \( N_v \) and \( F_e \) and thus, the accumulated soil data from past site investigations, such as the SPT \( N_v \) and \( F_e \), can be easily introduced into the proposed method. Several methods to synthesize the different sources of the investigation data have been proposed (e.g., Nishimura et al., 2016; Cardarelli et al., 2014), and their applicability to the evaluation of the liquefaction probability should be studied.

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