

# Geotechnical site characterization : recent improvements to assess one-dimensional consolidation settlements

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**ABSTRACT:** Working on Janbu's proposals, for the assessment of one-dimensional consolidation settlement for saturated soils, and on Boulanger and Idriss soil behaviour index to assess liquefaction susceptibility, it appears that soil can be classified in three families, having each their own set of relationships.

First, it is interesting to analyse if the  $400\mu\text{m}$ .D part is scattered in the  $0.400\mu\text{m}$  one, or if the  $400\mu\text{m}$ .D grains are in contact with each other's, D being the smaller dimension of the bigger grains.

Secondly, is introduced and analysed the interest of blue methylene values measurements. And then, having well characterised soil identification (gradation curve, blue methylene test, Atterberg limit, water content) is detailed how soils behave for each family, showing the complementary interest of cone penetration tests with induced pore water pressure measurement (CPT'u) and Menard pressuremeter test (PMT) for the first two categories.

**RESUME :** Travaillant sur les propositions de Janbu pour le calcul des tassements de consolidation unidimensionnelle des sols saturés et sur l'indice de susceptibilité à la liquéfaction de Boulanger et Idriss, il apparaît que les sols peuvent être classés en trois familles, ayant chacune leur propre jeu de relations.

Tout d'abord, il est intéressant d'analyser si la fraction  $400\mu\text{m}$ .D est disséminée dans celle  $0.400\mu$  ou si les grains  $400\mu\text{m}$ .D se touchent, D étant le diamètre le plus petit des plus gros grains.

Deuxièmement, la mesure des valeurs au bleu de méthylène d'un sol est une donnée intéressante. Et alors, ayant bien caractérisé l'identification du sol (analyse granulométrique, essai au bleu, limite d'Atterberg, teneur en eau) est détaillé comment les sols se comportent dans chaque famille, en montrant l'intérêt d'essais complémentaires de type essais au pénétromètre avec mesure de la pression interstitielle (CPT'u) et essais au pressiomètre Ménard (PMT) pour les deux premières familles.

**Keywords:** soil identifications ; oedometer tests ; one-dimensional consolidation settlement ; cone penetration tests with induced pore water pressure measurements (CPT'u) ; Menard pressuremeter tests (PMT).

## 1. Introduction

Geotechnical engineers have very often to assess one-dimensional consolidation settlements under mat foundations or embankments for example.

It is a source of miscalculations the wrong parameters being used. Recent improvements have been made, using and improving Janbu's proposals.

First, we will analyse, for a given  $2\mu\text{m}$  D soil, D being the smaller dimension of the greater grains – either when the grains  $400\mu\text{m}$ .D are scattered in the  $2\mu\text{m}$ . $400\mu\text{m}$  part, and when they are in contact with each other.

Secondly, the interest of the blue methylene test will be detailed.

And then, is presented, for each Janbu's soil family, all the relations we need in order to assess one-dimensional consolidation settlements.

When we write OD, it means soil granulometry starts at  $2\mu\text{m}$  and finishes at a diameter equal to D in mm. If we write d, d is an intermediate diameter.

## 2. $400\mu\text{m}$ .D grains scattered or not in the $2\mu\text{m}$ . $400\mu\text{m}$ part

Considering a soil, which grain sizes vary from  $2\mu\text{m}$  to D, gradation curve gives the percent passing in weight at  $400\mu\text{m}$ , we will write %400 $\mu$ . It is the passing on which Atterberg limits are measured, and here liquidity limit  $W_L$  and plasticity index PI will be used.

Oedometer tests are very often completed on this fraction, the greater size in the oedometer apparatus being limited to  $h/6$ , h height of the tested sample (usually  $h/6$  is equal to 3.1 mm).

Looking at figure n°1, it results that the dry bulk density  $\gamma_{d-O.D}$  of the O.D soil, is linked to the percent passing %400 $\mu$  and to the dry bulk density of the  $0.400\mu\text{m}$  fraction, through the expression :

$$\frac{1}{\gamma_{d\ 0.400\mu}} = \frac{\%400\mu}{\gamma_{d\ 0.400\mu}} + \frac{1-\%400\mu}{\gamma_s} \quad (1)$$

$\gamma_s$  being the average bulk density of the grains ( $\approx 27\text{kN/m}^3$ ).

$\gamma_{d\ 0.400\mu}$  dry bulk density of the  $0.400\mu\text{m}$  fraction.

weight	soil	volume
$\%400\mu \cdot \gamma_{d\ 0.400\mu}$	voids + $0.400\mu\text{m}$ grains	$\%400\mu \cdot \frac{\gamma_{d\ 0.400\mu}}{\gamma_{d\ 0.400\mu}}$
$(1-\%400\mu) \gamma_{d\ 0.400\mu}$	$400\mu\text{m.D}$ grains	$(1-\%400\mu) \frac{\gamma_{d\ 0.400\mu}}{\gamma_{d\ 0.400\mu}}$
$\gamma_{d\ 0.400\mu}$	Total	1

Figure n°1 : Soil partition at  $400\mu\text{m}$

Two situations are then possible :

- the  $400\mu\text{m.D}$  grains are scattered in the  $0.400\mu\text{m}$  part,
- the  $400\mu\text{m.D}$  grains are in contact with each others.

Let us examine the last case, through figure n°2:

Distribution of the $400\mu\text{m.D}$ grains	Volume	weight	
	Void Index $e_{0.400\mu}$	voids	0
	$\%400\mu$	grains $0-400\mu\text{m}$	$\%400\mu \cdot \gamma_s$
	$1-\%400\mu$	grains $400\mu\text{m.D}$	$(1-\%400\mu) \cdot \gamma_s$

Figure n°2 :  $400\mu\text{m.D}$  grains in contact

If the void index is  $e_{0.400\mu}$ , the total volume of the grains being 1:

- the available volume for the void  $e_{0.400\mu}$  and for the  $\%400\mu$  is :  $e_{0.400\mu} + \%400\mu$  (2)
- the weight of the  $0.400\mu$  is :  $\gamma_s \times \%400\mu$  (3)

and then the bulk density  $\gamma_{d\ 0.400\mu}$  is given by :

$$\gamma_{d\ 0.400\mu} = \frac{\%400\mu \times \gamma_s}{e_{0.400\mu} + \%400\mu} \quad (4)$$

We can write :

$$\%400\mu = e_{0.400\mu} \cdot \frac{\gamma_{d\ 0.400\mu}}{\gamma_s - \gamma_{d\ 0.400\mu}} \quad (5)$$

En figure n°3, we have drawn the curves  $\%400\mu$  as a function of bulk density  $\gamma_{d\ 0.400\mu}$ , for different values of  $e_{0.400\mu}$ : 0.17 ; 0.2 ; 0.25 ; 0.3 ; 0.4 ; 0.6 and 0.8 (dotted line).

Moreover, the volume occupied by the voids  $e_{0.400\mu}$  and the  $400\mu\text{m}$  passing must be less than the half of the total volume, if  $400\mu\text{m.D}$  grains are in contact ; that implies :

$$e_{0.400\mu} + \%400\mu \leq 0.5 (1 + e_{0.400\mu}) \quad (6)$$

$$\text{And then } \%400\mu < 0.5(1 - e_{0.400\mu}) = \frac{\gamma_{d\ 0.400\mu}}{\gamma_s + \gamma_{d\ 0.400\mu}} \quad (7)$$

The corresponding curve is drawn with a thick dashed line.

In a continuous line, is highlighted the curve corresponding to  $e_{0.400\mu}$  equal to 0.17 being the inferior limit under which it is very rare to have bulk densities greater than  $23\text{kN/m}^3$ .

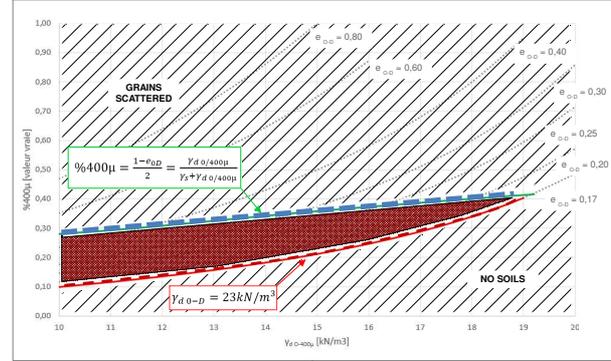


Figure n°3 : In dark zone  $400\mu\text{m.D}$  grains are in contact

On figure n°3, we have three areas:

- Lower one, no points (density too high),
- Intermediate one in grey:  $400\mu\text{m.D}$  grains are in contact,
- Upper zone:  $400\mu\text{m.D}$  grains are scattered.

We have shown [11] that when  $400\mu\text{m.D}$  grains are scattered,  $\gamma_{d\ 0.400\mu}$  is linked to  $\gamma_s$ ,  $VB_{0.400\mu}$ ,  $\sigma'_{vo}$  overburden effective vertical pressure and  $\sigma'_p$  preconsolidation pressure, through the relationship :

$$\frac{1}{\gamma_{d\ 0.400\mu}} = 0.445 + 0.02 \times (1.37 + VB_{0.400\mu}) \times (4.2 - \log(\sigma'_{vo}{}^{0.2} \cdot \sigma'_p{}^{0.8})) \quad (8)$$

When  $400\mu\text{m.D}$  grains are in contact, then  $\gamma_{d\ 0.400\mu}$  is probably lower than this value, due to possible arching effects through the  $400\mu\text{m.D}$  grains.

$VB_{0.400\mu}$  is the blue methylene value of the  $0.400\mu\text{m}$  fraction.

### 3. Interests of the blue methylene test

The blue methylene test is very often used in France, in soil identification, in order to characterize fines plasticity. The test allows to quantify the quantity of dry blue methylene noted  $VB_{0.400\mu}$ , that coats the internal and external surface of the clayey minerals of  $100\text{g}$  of  $0.400\mu\text{m}$  soils,  $d$  being an intermediate value between  $2\mu\text{m}$  and  $D\text{mm}$ .

And we can write :

$$VB_{0.400\mu} = \%d \times VB_{0.400\mu} = \%2\mu \times VB_{2\mu} \quad (9)$$

For french soils,  $VB_{0.400\mu}$  is well correlated to  $w_L$  and  $PI$  through the expression :

$$w_L = (1 - \%2\mu) \times 0.20 + 0.063 \times VB_{0.400\mu} \quad (10)$$

$$PI = -(1 - \%2\mu) \times 0.04 + 0.045 \times VB_{0.400\mu} \quad (11)$$

Knowing  $w_L$  and  $PI$ , it is possible to assess  $\%2\mu$ , value in percent of the passing at  $2\mu\text{m}$ .

Working on soil susceptibility to liquefaction, Boulanger and Idriss have noticed that soil behaviour was linked to an index noted  $S_{BI}$  :

$$S_{BI} = \frac{1}{\left[1 + \left(\frac{PI}{6.4}\right)^{8.2}\right]} \quad (12)$$

Figure n°4 shows the variation of  $1-S_{BI}$  as a function of PI, Boulanger and Idriss putting forward that for  $1-S_{BI}$  equal to zero the soil behaviour is sand like, that is for PI less than 3 and when equal to one is clay like, that is for PI greater than 8.

The corresponding values of  $VB_{0.400\mu}$  for a %2 $\mu$  equal to 30% are equal to respectively 1.3 and 2.4.

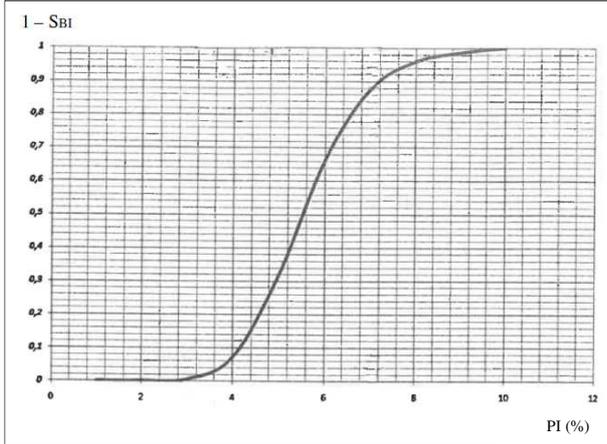


Figure n°4 : Boulanger and Idriss, soil behaviour index variation

#### 4. Theory of Janbu extended by Gress

Janbu et al. [2] have proposed for saturated soft soils that one dimensional settlements could be assessed through the relationship:

$$\frac{d\varepsilon}{d\sigma} = \frac{1}{m\sigma r} \left(\frac{\sigma_r}{\sigma'}\right)^{1-j} = \frac{1}{Mt} \quad (13)$$

$m$  = Janbu modulus;  $j$  = stress exponent;  $\sigma_r = 100$  kPa;  $\sigma$  = strain;  $\varepsilon$  = deformation,  $Mt$  tangent modulus.

To extend this proposal, we suggest to write :  $j = S_{BI}$

When, as shown in paragraph 2,  $400\mu.D$  grains are in contact one with each others, we suggest that for Janbu, these soils belong to category 1.

If, on the contrary,  $400\mu.D$  grains are scattered then the  $0.400\mu$  fraction belongs to category 1 if PI is less than 3, to category 2 if it is between 3 and 8, and to category 3 if PI is greater than 8.

And then :

- Soil category 1 : for  $PI < 3$ , we have  $1 - j = 0$

$$\varepsilon = \frac{1}{m\sigma_r} \Delta\sigma \quad (14)$$

- Soil category 2 :  $3 \leq PI \leq 8$   
For example when  $PI = 4.5$   $i = S_{BI} = 0.5$

and then if  $\sigma'_v > \sigma'_p$  :

$$\varepsilon = \frac{1}{5m_r} \left(\sqrt{\sigma'_p} - \sqrt{\sigma'_{vo}}\right) + \frac{1}{5m} \left(\sqrt{\sigma'_v} - \sqrt{\sigma'_{vo}}\right) \quad (15)$$

If not :

$$\varepsilon = \frac{1}{5m_r} \left(\sqrt{\sigma'_v} - \sqrt{\sigma'_{vo}}\right) \quad (16)$$

- Soil category 3 : for  $1-j = 1$  and if  $\sigma'_v > \sigma'_p$

$$\varepsilon = \frac{1}{m_r} \text{Ln} \left(\frac{\sigma'_p}{\sigma'_{vo}}\right) + \frac{1}{m} \text{Ln} \left(\frac{\sigma'_v}{\sigma'_p}\right) \quad (17)$$

With :

$$m = \text{Ln} 10 \frac{1+eo}{Cc} \quad m_r = \text{Ln} 10 \frac{1+eo}{Cs} \quad (18)$$

If not :

$$\varepsilon = \frac{1}{m_r} \text{Ln} \left(\frac{\sigma'_v}{\sigma'_{vo}}\right) \quad (19)$$

where :  $\sigma'_v$  final effective stress (kPa) ;  $\sigma'_p$  preconsolidation pressure (kPa) ;  $\sigma'_{vo}$  initial effective stress (kPa) ;  $m$  Janbu modulus (dimensionless) ;  $m_r$  recompression modulus number (dimensionless).

#### 5. One-dimensional consolidation settlement of category 1 and 2 soils.

Massarsch (1994) – Menard (1958) – Gress (2019)

Massarsch [6] has proposed a relationship, giving the value of  $m$ , knowing the cone tip resistance  $qt$  during a static cone penetration test :

$$m = a \frac{qt^{0.5}}{(\sigma_r \sigma'_{vo})^{0.25}} \quad (20)$$

$qt$ ,  $\sigma'_{vo}$  in kPa,  $\sigma_r = 100$  kPa and  $a$  being an empirical parameter, function of soil nature and it's compacity.

Gress et al. [6] have recently proposed the expression hereafter for a :

$$a = \frac{1}{\alpha_M} \frac{\sigma'_{vo}{}^{0.25}}{\sigma_r{}^{0.75}} qt^{0.54} \text{ in kPa} \quad (21)$$

fitting with the values proposed by Massarsch,  $\alpha_M$  varying here from 0.33 to 0.61 through :

$$\alpha_M = 0.33(2-j) \quad (22)$$

Then we can write  $m$   $\sigma_r$  as :

$$M_t = m \sigma_r = \frac{3}{2 \alpha_M} qt^{1.04} \quad (23)$$

Moreover having noticed [7] a good correlation between  $q_T$  and Menard PMT parameters, that is :  $pl^*$  net limit pressure and  $E_M$  Menard modulus, given by the relationships here after :

$$q_T = (pl^*)^{1.25} \quad E_M = (pl^*)^{1+\alpha} \text{ in kPa, with } \alpha = 0.4 \frac{VB_{OD} + 0.7}{VB_{OD} + 1} \quad (24)$$

$m\sigma_r$  becomes then :

$$m\sigma_r = \frac{3}{2\alpha_M} E_M \quad (25)$$

K can be written for  $\nu = 0.33$  :

$$3K = \frac{1+\nu}{1-\nu} M_t \approx 2M_t \quad (26)$$

knowing that ((27) and (28)) :

$$M_t = \frac{(1-\nu)}{(1+\nu)(1-2\nu)} Et \quad \text{and} \quad K = \frac{Et}{3(1-2\nu)}$$

When  $1-j = 0$ , then  $M_t = m\sigma_r$   
and the value of K becomes :

$$K = \frac{E_M}{\alpha_M} = \frac{q_T^{1.04}}{\alpha_M} \quad \text{in kPa} \quad (29)$$

Distributed loads at soil surface on a large area, induces one-dimensional deformation given through:

$$\varepsilon_{zz} = \frac{\bar{\sigma}_i}{K} \quad (30)$$

with :

$$\bar{\sigma}_i = \frac{\bar{\sigma}_{xx} + \bar{\sigma}_{yy} + \bar{\sigma}_{zz}}{3} \quad (31)$$

## 6. One-dimensional consolidation settlement of category (3) soils

### 6.1. Soils with dimensions of grains less than 400 $\mu\text{m}$

The assessment of settlements is here conducted using relations (17) and (19).

The parameters  $m$ ,  $m_r$  and  $\sigma'_p$  are generally measured through oedometer tests, with :

$$m = Ln 10 \frac{1+eo}{Cc} \quad m_r = Ln 10 \frac{1+eo}{Cs} \quad (32)$$

where :

$e_0$  = initial void index ;  $Cc$  = compression index ;  $Cs$  = swelling index ;  $\sigma'_p$  = preconsolidation pressure.

Two major difficulties are :

- the quality of the intact samples,
- the limit of the maximum value of the grains in the sample generally fixed at 3mm ( $\frac{19}{6}$ ) for an oedometer test.

It is then interesting to have some correlations as :

$$Cc = 0.9 (W_L - 0.1) \text{ Terzaghi (1967)} \quad (33)$$

$W_L$  for its real value for 0-400 $\mu\text{m}$  samples, or:

$$Cc = 2.7 \frac{W_{SC} - 0.075}{4.2 - \log(\sigma'_{vo}{}^{0.2} \sigma'_p{}^{0.8})} \quad [4] \quad (34)$$

$W_{SC}$  water content in the overconsolidation state, expression due to Gress, derived from Herrero.

$$Cs \approx 0.2 Cc \quad (35)$$

Preconsolidation pressure is also a very difficult parameter to measure. It is interesting to compare the laboratory results to the correlations hereafter [5]:

$$\sigma'_{vo}{}^{0.2} \sigma'_p{}^{0.8} = (q_T - \sigma'_v)^{0.8m} = (p1^*)^m \quad (36)$$

$m$  Mayne factor equal to

$$m = 1 - 0.28 \frac{1}{1 + (Ic / 2.65)^{25}} \quad (37)$$

With :  $Ic = 3.6 \frac{W_L - 0.115}{W_L - 0.025}$   $Ic$  Robertson behavior index, that is also or given through the CPT'u parameters. (38)

The value of settlement is calculated at the end of the primary consolidation at a time  $tp$ .

Finally, creep has to be taken account for:

$$\varepsilon_{zzf} = \frac{c_\alpha}{1 + e_p} \log \frac{tf}{tp} \quad (39)$$

$$C_\alpha \text{ creep index} \approx 0.04 Cc \quad (40)$$

$e_p$  void index at the end of the primary consolidation;  
 $tf \approx 10$  years ;  $tp$  in year

### 6.2. Complete O.D soils (granulometry from 2 $\mu\text{m}$ to D mm)

For a O.D soils, looking at figure n° 2, we can write

$$e_{0,400\mu} = \frac{e_{O,D}}{\%400\mu} \quad (41)$$

$$\text{or } e_{O,D} = \%400\mu \cdot e_{0,400\mu} \quad (42)$$

$$\text{and then : } \Delta e_{O,D} = \%400\mu \cdot \Delta e_{0,400\mu} \quad (43)$$

this means that :

$$C_{S_{O,D}} = C_{S_{0,400\mu}} \cdot \%400\mu \quad (44)$$

$$C_{C_{O,D}} = C_{C_{0,400\mu}} \cdot \%400\mu \quad (45)$$

$$\text{And : } \sigma'_{p-O,D} = \sigma'_{p-0.400\mu} \quad (46)$$

where  $C_s$  swelling index,  $C_c$  compression index, and  $\sigma'_p$  preconsolidation pressure.

### 6.3. Conclusions

Having to assess one consolidation settlement, we have presented steps and relationships allowing to have relevant values of the parameters we need.

Proposed correlations are fitted to french experience, for saturated soils, having a sensitivity less than 4. For other countries, it is necessary to confront proposed values to local experience.

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